# TOROS ÜNIVERSITESI 

Faculty Of Engıneering
Industrial Engıneering (English)
Course Information

| PROBABILITY THEORY |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Code | Semester | Theoretical |  | Practice | National Credit |
|  |  | Hour $/$ Week |  | ECTS Credit |  |
| MAT202 | Spring | 3 | 0 | 3 | 4 |


| Preqequisites and co- <br> requisites | MAT103 |
| :--- | :--- |
| Language of instruction | English |
| Type | Required |
| Level of Course | Bachelor's |
| Lecturer | Assit. Prof. Dr. Türker Ertem |
| Mode of Delivery | Face to Face |
| Suggested Subject | None |
| Professional practise ( <br> internship ) | None |
| Objectives of the Course | For students seeking an introduction to probability theory and applications without any prerequisites, this <br> course is designed to develop their intuition and model building skills. They will develop ways of thinking in <br> formal reasoning (intuitively understand a number of fundamental probabilistic reasoning concepts based <br> on a mathematical foundation). They also learn how to solve real world problems under uncertainty by <br> structuring them, building models, and analyzing those models. |
| Contents of the Course | Events and probability. Combinatorial problems. Independence and conditional probability. Measure <br> theoretical approach to probability. Random variables and distribution functions. Marginal distributions and <br> conditional distributions. Moments and characteristic functions. Convergence of random variables. Law of <br> large numbers. |

## Learning Outcomes of Course

| $\#$ | Learning Outcomes |
| :--- | :--- |
| 1 | Students will be able to define the relevant random events of a random experiment and to compute the probabilities of simple and <br> composition of events |
| 2 | Students will be able to check the independence of events, to compute the conditional probabilities, and to use Bayes' Theorem. |
| 3 | Students will be able to compute probabilities related to a random variable, expected value and variance of a random variable using <br> probability mass function, probability density function, cumulative distribution function. |
| 4 | Students will know and use properties of some well-known discrete and continuous probability distributions. |
| 5 | Students will be able to use joint distributions to compute probabilities of events in more than one random variable, to compute marginal <br> distributions, and to compute the distributions of functions of two random variables. |
| 6 | Students will know properties of random samples and the distributions of the sample mean and sample variance. |

Course Syllabus

| $\#$ | Subjects | Teaching Methods <br> and Technics |
| :--- | :--- | :--- |
| 1 | I. Combinatorial Analysis 1.1 Introduction 1.2 The Basic Principle of Counting 1.3 Permutations | Lecturing |
| 2 | 1.4 Combinations 1.5 Multinomial Coefficients 1.6 The Number of Integer Solutions of Equations | Lecturing |
| 3 | II. Axioms of Probability 2.1 Introduction 2.2 Sample Space and Events 2.3 Axioms of Probability | Lecturing |
| 4 | 2.4 Some Simple Propositions 2.5 Sample Spaces Having Equally Likely Outcomes | Lecturing |


| 5 | 2.6 Probability as a Continuous Set Function 2.7 Probability as a Measure of Belief | \| Lecturing |
| :---: | :---: | :---: |
| 6 | III. Conditional Probability and Independence 3.1 Introduction 3.2 Conditional Probabilities 3.3 Bayes's Formula | Lecturing |
| 7 | 3.4 Independent Events 3.5 P( $\cdot \mid F)$ Is a Probability | Lecturing |
| 8 | IV. Random Variables 4.1 Random Variables 4.2 Discrete Random Variables 4.3 Expected Value | Lecturing |
| 9 | 4.4 Expectation of a Function of a Random Variable 4.5 Variance 4.6 The Bernoulli and Binomial Random Variables | Lecturing |
| 10 | 4.7 The Poisson Random Variable 4.8 Other Discrete Probability Distributions 4.9 Expected Value of Sums of Random Variables 4.10 Properties of the Cumulative Distribution Function | Lecturing |
| 11 | V. Continuous Random Variables 5.1 Introduction 5.2 Expectation and Variance of Continuous Random Variables 5.3 The Uniform Random Variable 5.4 Normal Random Variables | Lecturing |
| 12 | 5.5 Exponential Random Variables 5.5.1 Hazard Rate Functions 5.6 Other Continuous Distributions 5.7 The Distribution of a Function of a Random Variable | Lecturing |
| 13 | VI. Jointly Distributed Random Variables 6.1 JointDistributionFunctions 6.2 Independent Random Variables 6.3 Sums of Independent Random Variables 6.4 Conditional Distributions: Discrete Case | Lecturing |
| 14 | 6.5 Conditional Distributions: Continuous Case 6.6 Order Statistics 6.7 Joint Probability Distribution of Functions of Random Variables 6.8 Exchangeable Random Variables | Lecturing |
| 15 |  |  |
| 16 | Final Exam |  |

## Course Syllabus

| $\#$ | Material / Resources | Information About <br> Resources | Reference / Recommended <br> Resources |
| :--- | :--- | :--- | :--- |
| 1 | Ross, Sheldon M. A first course in probability, 8th Edition |  |  |
| 2 | Girimmet, Stirzaker, Probability and Random Processes, Oxford <br> University Press, (2001) |  |  |

## Method of Assessment

| $\#$ | Weight | Work Type | Work Title |
| :--- | :--- | :--- | :--- |
| 1 | $40 \%$ | Mid-Term Exam | Mid-Term Exam |
| 2 | $60 \%$ | Final Exam | Final Exam |

## Relationship between Learning Outcomes of Course and Program Outcomes

| $\#$ | Learning Outcomes | Program <br> Outcomes | Method of <br> Assessment |
| :--- | :--- | :--- | :--- |
| 1 | Students will be able to define the relevant random events of a random experiment and to compute the <br> probabilities of simple and composition of events | 1,7 |  |
| 2 | Students will be able to check the independence of events, to compute the conditional probabilities, and to use <br> Bayes' Theorem. | 1,7 | 1,2 |
| 3 | Students will be able to compute probabilities related to a random variable, expected value and variance of a <br> random variable using probability mass function, probability density function, cumulative distribution function. | 1,7 | 1,2 |
| 4 | Students will know and use properties of some well-known discrete and continuous probability distributions. | 1,7 | 1,2 |
| 5 | Students will be able to use joint distributions to compute probabilities of events in more than one random <br> variable, to compute marginal distributions, and to compute the distributions of functions of two random <br> variables. | 1,7 | 1,7 |
| 6 | Students will know properties of random samples and the distributions of the sample mean and sample <br> variance. | 1,2 |  |

PS. The numbers, which are shown in the column Method of Assessment, presents the methods shown in the previous table, titled as Method of Assessment.

## Work Load Details



